

# Assessing the Appropriate Size of Relief in Sovereign Debt Restructuring

LACEA, Buenos Aires

Martin Guzman (Columbia-UBA-CIGI)    Domenico Lombardi (Oxford  
Institute for Economic Policy)

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- What's the “appropriate” size of relief in a sovereign debt restructuring process?

- The ultimate goal of a sovereign restructuring is the restoration of *debt sustainability*
  - But there may be more relevant constraints than just the government's transversality condition for defining *debt sustainability*
    - Principles-based approach for assessing debt sustainability

- Evidence shows that sovereign debt restructuring processes are being ineffective at restoring sustainability

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<b>Fraction</b>	0.497	0.525	0.553	0.575	0.6

- Fraction: denotes fraction of restructuring with private creditors (bondholders and bank loans) followed by another restructuring or default with the same group within  $t$  years

- Evidence shows that sovereign debt restructuring processes are being ineffective at restoring sustainability

$t$	3	4	5	6	7
<b>High Income</b>	0.619	0.650	0.700	0.700	0.700
<b>Upper Middle Income</b>	0.500	0.548	0.578	0.590	0.622
<b>Lower Middle Income</b>	0.467	0.477	0.500	0.523	0.548
<b>Low Income</b>	0.455	0.455	0.469	0.531	0.548
<b>Total</b>	0.497	0.525	0.553	0.575	0.6

- Fraction: denotes fraction of restructuring with private creditors (bondholders and bank loans) followed by another restructuring or default with the same group within  $t$  years

- Evidence is very suggestive of a too little syndrome
- Suppose that the actual probability that a restructuring with private creditors is followed by another restructuring or default with the same group within five years is 0.05, and that that variable follows a Poisson distribution
- Then, probability of observing  $Fraction = 0.553$  for  $t = 5$  (i.e. probability of observing 95 failed attempts at resolving the sovereign debt crises in a sample of 179 episodes) would be equal to  $5.37 \times 10^{-62}$  – an extremely rare event

- Flawed approach: Inter-country comparison of market haircuts (Edwards 2015)
  - 180 restructuring episodes with private creditors from 1970 to 2010 (data from Cruces-Trebesch 2013)
  - Actual haircuts vs. Predicted haircuts

$$H_t = 1 - \frac{PV \text{ new bond}(r_{t+\epsilon})}{PV \text{ old bond}(r_{t+\epsilon})}$$

- If actual haircut  $>>$  ( $<<$ ) predicted haircut  $\implies$  too much (too little) haircut

The relief is appropriate if it restores sustainability  
*with high probability*

# A methodology for assessing the appropriate size of relief in sovereign debt restructuring

- Define the relevant constraints:
  - The Government's Intertemporal Budget Constraint (GIBC)
  - The principles-based constraints
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- First, define GIBC:

$$d_t^* = \sum_{j=0}^{\infty} [1 + r(t, t+j)]^{-1} s_{t+j} | z_{\infty}^i$$

with

$$1 + r(t, t+j) = \prod_{k=0}^j (1 + r_{t+k})$$

and TC:

$$\lim_{j \rightarrow \infty} [1 + r(t, t+j)]^{-1} d_{t+j} | z_{\infty}^i$$

- Suppose:

$$s_t = s(\gamma_t, R_t, X_t^s, \epsilon_t^s)$$

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- For each possible economic scenario, find the trajectory of fixed points for the primary fiscal balance that satisfies GIBC

### Definition 1

*The set of economically feasible  $s_t$  is defined as*

$$J^E = \{s_t : \underline{\gamma(s_t, X_t^\gamma, \epsilon_t^\gamma) > -1 \wedge R(s_t, X_t^R, \epsilon_t^R) > \gamma(s_t, X_t^\gamma, \epsilon_t^\gamma)}\}$$

### Definition 2

*$s_t^*$  is an economically feasible fixed point if  $s_t^* \in J^E$*

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### Definition 2

*$s_t^*$  is an economically feasible fixed point if  $s_t^* \in J^E$*

- Check if each trajectory of fixed points respects the constraints imposed by the principles (political feasibility)
  - Trajectories of fixed points for the primary fiscal balance that the GIBC and the constraints imposed by the principles are *feasible*

### Definition 3

*The set of politically feasible  $s_t$  is defined as  $J^P$*

### Definition 4

*$s_t^*$  is a politically feasible fixed point if  $s_t^* \in J^P$*

### Definition 5

*$s_t^*$  is a feasible fixed point if  $s_t^* \in J^F = J^E \cap J^P$*

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- If there is a “sufficiently large” mass of *feasible* trajectories of fixed points, then the debt state satisfies sustainability with high probability
- Otherwise, there is need for a debt write off large enough as to achieve a “sufficiently large” mass of *feasible* trajectories of fixed points

## Definition 6

$d_{t-1,t}$  is x-sustainable if given the probability distributions for  $\epsilon_t^i$  ( $i = s, \gamma, R$ ), there are  $\{s_t^*\}_t \in J^F$  s.t. GIBC holds with probability mass not smaller than  $x$

## Definition 7

Suppose GIBC holds with probability  $x' < x$  for  $d_t^*$ . Then, the appropriate level of debt relief,  $\Delta$ , must satisfy  $\Delta = d_t^* - d_t^{*'},$  where  $d_t^{*'} is the maximum value of d that satisfies x-sustainability$

A methodology for assessing the appropriate size of relief in sovereign debt restructuring:

*An illustration of how to apply it*

- Commonly invoked object in practical episodes of restructuring: the debt-stabilizing constant fiscal surplus to GDP ratio
- Suppose  $\gamma_t = \gamma$ ,  $R_{t,t+1} = R$ , both r.v. ex-ante
- Let  $\gamma^n$  and  $R^n$  be any possible realization of  $\gamma$  and  $R$   
 $\implies$

$$s^n = d_t^* \left( \frac{R^n - \gamma^n}{1 + \gamma^n} \right)$$

- Suppose

$$\gamma^n = \alpha_0 - \alpha_1 s^n$$

$$R^n = \beta_0 - \beta_1 s^n$$

- $\alpha_i$  and  $\beta_i$  have discrete uniform distributions:  
 $\alpha_0 \sim \text{unif}(0.02, 0.07)$  with  $\text{pmf} = 1/6$ ;  $\alpha_1 \sim \text{unif}(0, 1)$  with  $\text{pmf} = 1/11$ ;  
 $\beta_0 \sim \text{unif}(0.03, 0.07)$  with  $\text{pmf} = 0.2$ ;  
 $\beta_1 \sim \text{unif}(0, 101)$  with  $\text{pmf} = 1/101$

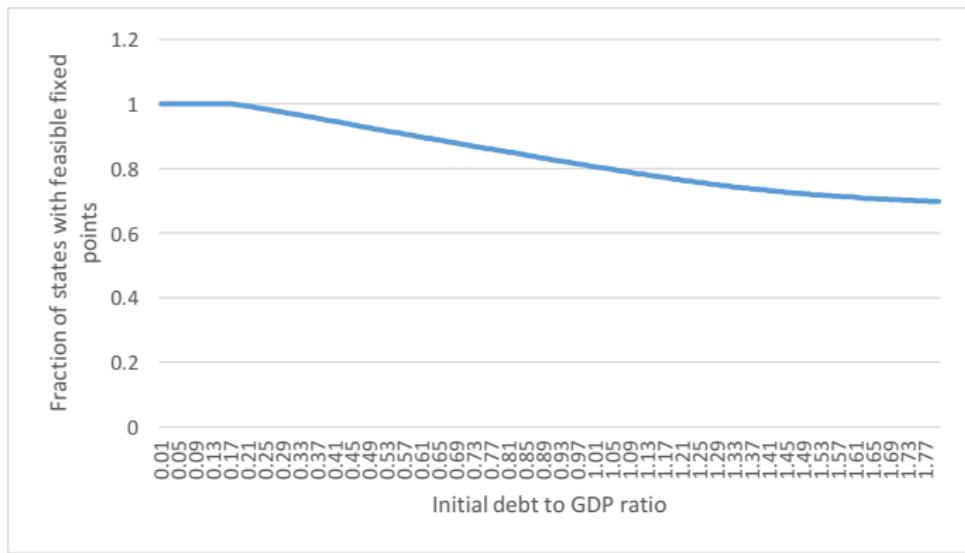
- Under our distributional assumptions,  $N = 33,330$  combination of states
- Compute  $s^n$  for each  $n$ , for  $d_t^* \in [0.01, 1.8]$ 
  - Multiple fixed points

- ① Eliminate dynamically inefficient combinations
- ② Count scenarios where there is at least one economically feasible fixed point
- ③ Political feasibility: suppose  
$$J^P = \{s_t \in (-1, 1) : \gamma(s_t, X_t^\gamma, \epsilon_t^\gamma) \geq 0.01\}$$
- ④ Count scenarios where there is at least one politically feasible fixed point
- ⑤ Compute ratio of relevant scenarios with feasible fixed point

# A criterion for assessing the appropriate size of debt relief

## An illustration: The case of constant fiscal surplus to GDP ratio

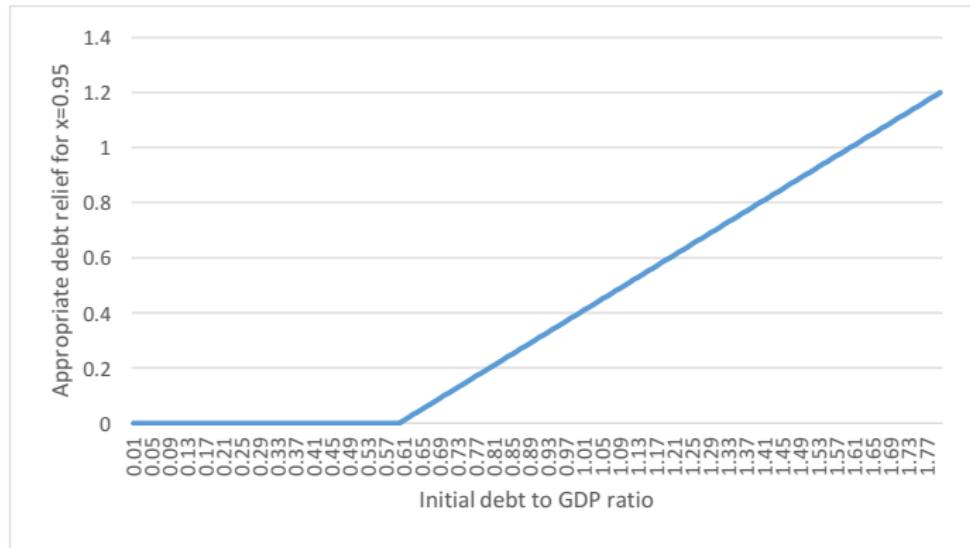
- x-sustainability:



# A criterion for assessing the appropriate size of debt relief

## An illustration: The case of constant fiscal surplus to GDP ratio

- Appropriate relief,  $x = 0.95$



- Computing the appropriate non-contingent relief requires knowledge on the distribution of fiscal multipliers
- Framework is complementary of IMF Fan Charts Approach  
(Abiad-Ostry 2005; Celasun-Debrun-Ostry 2006)
  - Fan Chart analysis helps to rule out via stress tests unusual predictions regarding variables over which uncertainty is high

- Need for clarifying what's a sensible framework for assessing how appropriate is a debt write-down
- Evidence that suggests presence of *too little* syndrome in sovereign debt restructuring
- Possible guide for practitioners
  - Framework could be the basis for the codification the UN *sustainability principle*